

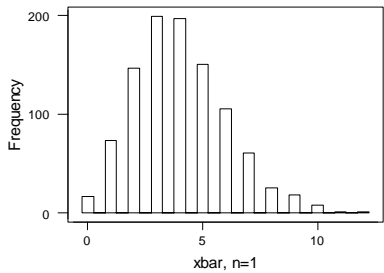
STA362: Introduction to Statistics

Illustration of sampling distribution characteristics

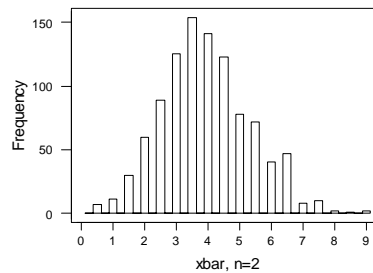
For a certain manufacturing industry, the *average number of industrial accidents per month* is sought. If we define Y = # of accidents per month, a good model for Y would be a Poisson distribution with parameter λ . What we want to find out is the true mean of Y . Since Y is Poisson, $\mu = \lambda$. Also, remember that the standard deviation of Y is $\sigma = \sqrt{\lambda}$. For the following simulation, let $\mu = \lambda = 4.0$.

Statistical strategy: Collect a sample of monthly data, and use \bar{x} from the sample to estimate μ (i.e., $\lambda = 4.0$ in this case). What is the key aspect of data collection that will affect the quality of the \bar{x} estimate?

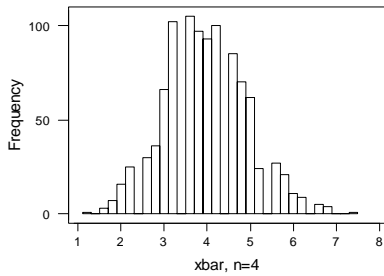
Simulation of sampling distribution of \bar{x} -bar



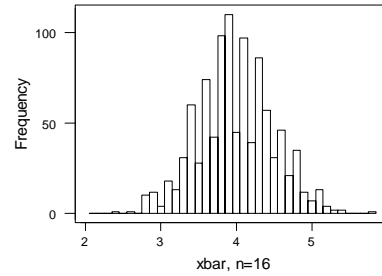
Simulation of sampling distribution of \bar{x} -bar



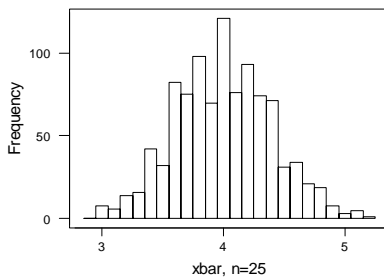
Simulation of sampling distribution of \bar{x} -bar



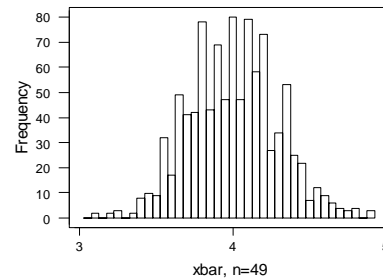
Simulation of sampling distribution of \bar{x} -bar



Simulation of sampling distribution of \bar{x} -bar



Simulation of sampling distribution of \bar{x} -bar



Descriptive Statistics for each simulated sampling distribution

	reps	Mean	Median	StDev
\bar{x} -bar, $n=1$	1000	4.0180	4.0000	2.0213
\bar{x} -bar, $n=2$	1000	3.9385	4.0000	1.4126
\bar{x} -bar, $n=4$	1000	3.9475	4.0000	0.9668
\bar{x} -bar, $n=16$	1000	3.9861	3.9375	0.4976
\bar{x} -bar, $n=25$	1000	4.0000	4.0000	0.3989
\bar{x} -bar, $n=49$	1000	4.0052	4.0000	0.2909